

"Frontmatter"
The Transform and Data Compression Handbook
Ed. K. R. Rao and P.C. Yip.
Boca Raton, CRC Press LLC, 2001

**THE
TRANSFORM
AND DATA
COMPRESSION
HANDBOOK**

**THE ELECTRICAL ENGINEERING
AND SIGNAL PROCESSING SERIES**
Edited by Alexander Poularikas and Richard C. Dorf

Handbook of Antennas in Wireless Communications
Lal Chand Godara

Propagation Data Handbook for Wireless Communications
Robert Crane

The Digital Color Imaging Handbook
Guarav Sharma

Handbook of Neural Network Signal Processing
Yu Hen Hu and Jeng-Neng Hwang

Handbook of Multisensor Data Fusion
David Hall

*The Advanced Signal Processing Handbook:
Theory and Implementation for Radar, Sonar,
and Medical Imaging Real Time Systems*
Stergios Stergiopoulos

The Transform and Data Compression Handbook
K.R. Rao and P.C. Yip

The Encyclopedia of Signal Processing
Alexander Poularikas

Applications in Time Frequency Signal Processing
Antonia Papandreou-Suppappola

THE TRANSFORM AND DATA COMPRESSION HANDBOOK

Edited by

K.R. RAO

University of Texas at Arlington

AND

P.C. YIP

McMaster University



CRC Press

Boca Raton London New York Washington, D.C.

Library of Congress Cataloging-in-Publication Data

The transform and data compression handbook / editors, P.C. Yip, K.R. Rao.

p. cm.--(Electrical engineering and signal processing series)

Includes bibliographical references and index.

ISBN 0-8493-3692-9 (alk. paper)

1. Data transmission systems--Handbooks, manuals, etc.. 2. Data compression (Telecommunication)--Handbooks, manuals, etc. I. Yip, P.C. (Pat C.) II. Rao, K. Ramamohan (Kamisetty Ramamohan) III. Series

TK5105 .T72 2000

621.382--dc21

00-057149

This book contains information obtained from authentic and highly regarded sources. Reprinted material is quoted with permission, and sources are indicated. A wide variety of references are listed. Reasonable efforts have been made to publish reliable data and information, but the author and the publisher cannot assume responsibility for the validity of all materials or for the consequences of their use.

Neither this book nor any part may be reproduced or transmitted in any form or by any means, electronic or mechanical, including photocopying, microfilming, and recording, or by any information storage or retrieval system, without prior permission in writing from the publisher.

All rights reserved. Authorization to photocopy items for internal or personal use, or the personal or internal use of specific clients, may be granted by CRC Press LLC, provided that \$.50 per page photocopied is paid directly to Copyright Clearance Center, 222 Rosewood Drive, Danvers, MA 01923 USA. The fee code for users of the Transactional Reporting Service is ISBN 0-8493-3692-9/00/\$0.00+\$.50. The fee is subject to change without notice. For organizations that have been granted a photocopy license by the CCC, a separate system of payment has been arranged.

The consent of CRC Press LLC does not extend to copying for general distribution, for promotion, for creating new works, or for resale. Specific permission must be obtained in writing from CRC Press LLC for such copying.

Direct all inquiries to CRC Press LLC, 2000 N.W. Corporate Blvd., Boca Raton, Florida 33431.

Trademark Notice: Product or corporate names may be trademarks or registered trademarks, and are used only for identification and explanation, without intent to infringe.

© 2001 by CRC Press LLC

No claim to original U.S. Government works

International Standard Book Number 0-8493-3692-9

Library of Congress Card Number 00-057149

Printed in the United States of America 1 2 3 4 5 6 7 8 9 0

Printed on acid-free paper

Preface

While this handbook is an exposition of different discrete transforms and their ever-expanding applications in the general area of signal processing, the overriding task is to maintain the continuity and connectivity among the chapters. This task is accomplished by the common theme of data compression. The handbook seeks to provide the reader with a wealth of information regarding the transforms (some have been widely used while others have great potential) as well as a demonstration of their power and practicality in data compression. Such compression is a necessary and desirable ingredient in today's world of massive data storage and data transmission. By providing a plethora of Web sites, ftp locations, and references to general review papers, the chapter authors have expanded the usefulness of this handbook for the common reader. The clear and concise presentations of the ideas and concepts, as well as the detailed descriptions of the algorithms, provide important insights into the applications and their limitations. With the understanding of these concepts, readers can apply the techniques presented in this handbook to their own areas of interest and improve on the performance by marrying this with their own expertise. We are confident that this handbook will be a valuable addition to the bookshelf of anyone actively engaged in or studying the art and science of signal processing.

The Transform and Data Compression Handbook is aimed at providing a description of various discrete transforms and their applications in different disciplines. In view of the proliferation of digital data (images, video, text, documents, audio, music, graphics, etc.), it is imperative that the data be mapped from the data domain (in which there are usually redundancies) to a different one (the transform domain) for efficient and economical storage and/or transmission. Transforms by themselves do not provide any compression. However, by reallocation of the energy in the data, transforms provide the possibilities for compression. Techniques such as adaptive quantization and entropy coding applied to the transform coefficients can result in significant reduction in bit rates. Depending on the quality levels required by the end user, other parameters such as human visual/acoustic sensitivity, adaptive scanning, statistical modeling, and variable length coding would further contribute to the bit rate reduction. Generally transforms, wavelet transforms in particular, are well suited for scalable coding (in spatial or temporal domains, or in SNR). This concept facilitates data transmission in embedded bit-stream format, providing for multi-resolution (spa-

tial/temporal) and multiquality (SNR) end products, subject to bandwidth limitation, processing power, and cost constraints.

Many international standards relating to audio, video, and data, such as JPEG, H.261, H.262, MPEG-1, MPEG-2, MPEG-4, HDTV, and JPEG-2000, utilize transforms in their overall compression schemes. A number of consumer and commercial products, such as video-CD, DVD, videophone, set-top boxes, digital TV, and digital camera/VCR, have been made possible because of signal compression. Other electronic innovations, such as MP3, video-streaming, and wireless PCS, are completely dependent on the reduction of bit rates made possible by compression. It is not exaggerating to say that data compression is one of the main contributing factors in the explosive growth in information technology.

While different coding schemes can accomplish an amazing amount of compression, the cornerstone is still undoubtedly the underlying transform. It is for this reason that the definitions and properties for each of the transforms dealt with in this handbook are presented with such care and detail. The bibliography sections and Web sites provide further sources of information.

Outline of Chapters

Chapter 1 The Karhunen-Loève Transform

The first transform described in this handbook is the Karhunen-Loève transform (KLT). It takes its rightful place as the leadoff transform to be discussed. Dony does an excellent job of interpreting this statistically optimal transform. The simple and yet elegant explanation of rotation of axes in the data domain to achieve the “principal components” representation underscores the significant energy compaction provided by this transform. Other properties of the transform follow, and the chapter is rounded off with descriptions of applications in chest radiographs and other monochrome and color images. Web sites and software download locations are listed as well.

Chapter 2 The Discrete Fourier Transform

Discrete Fourier transform (DFT), the best known and arguably the most universally applied transform, is presented by Selesnick and Schuller. Following an exposition of the definitions and properties of the DFT, it is shown that by a symmetric extension of the sequence, the DFT can lead to the discrete cosine transform (DCT), another favorite transform described in Chapter 4. The authors then go on to develop the fast Fourier transform (FFT) algorithms, a catalyst for all DFT applications. A novel feature of this chapter is the linkage provided by the authors between DFT and filter-banks, which are used extensively in audio coders. Cosine-modulated filter-banks and complex DFT-based filter-banks are the byproducts of the DFT that are used in Moving Picture Expert Group (MPEG) audio coders. There is an extensive list of Web sites providing information for available software, algorithms, and applications, as well as other related links.

Chapter 3 Comparametric Transforms for Transmitting Eye Tap Video with Picture Transfer Protocol (PTP)

This is a unique, challenging, and provocative chapter written by Mann, the inventor of the wearable computer (WearComp), the Eye Tap camera, and reality mediator. This chapter takes us to the forefront of the multimedia revolution with a new computational/communications device that subsumes the functionality of the videophone, digital camera, and other wireless personal electronics innovations. Mann's invention functions as a true extension of the mind and body and causes the eye to function as if it were a camera. His invention has given rise to a whole new philosophical and mathematical approach to image compression and image storage, and it gives a refreshingly new definition of functionality in image transmission and processing. The new Eye Tap genre of video is best processed and compressed by comparametric equations, essentially equations representing projections and tone scale adjustments of images. Traditionally image compression has been directed to ensure a certain minimum quality or reliability (e.g., worst case scenario). The author instead makes a compelling argument in favour of "best case" scenario; Mann argues that being able to broadcast even intermittent still images to the Internet can provide a measure of security unmatched by conventional "robust" security systems. These arguments are based on a definition of "fear of functionality," a completely novel approach to the idea of security. The author has set up a Web site from which computer programs can be freely downloaded. Such a generous spirit is to be commended. It is also interesting to note that this chapter was typeset using LaTeX running on a small wearable computer designed and built by the author.

Chapter 4 Discrete Cosine and Sine Transforms

Next to the DFT, discrete cosine transform (DCT) is probably the most used transform in digital signal processing work. DCT is one of a family of trigonometric transforms including the discrete sine transform (DST). In this chapter, Britanak presents a unified treatment of the family of DCTs and DSTs starting with the definitions, properties, and fast algorithms. This chapter is particularly relevant as the DCT has been adopted in several international standards for image/video coding. In modified form, both DCT and DST have been used in MDCT/MDST audio coding. Computer programs in C (listed in Sections 4.3 and 4.4) that can be implemented to perform the transforms are very useful in all signal processing applications. The chapter concludes with a specific application in a Joint Photographic Experts Group (JPEG) base line system (Fig. 4.3) using the standard test image of Lena.

Chapter 5 Lapped Transforms for Image Compression

Lapped transforms (LTs), developed originally to eliminate or reduce the blocking artifacts of block transforms such as DCT in low bit rate image/video coding, are presented by de Queiroz and Tran. Several versions of the LTs, such as orthogonal and nonorthogonal LTs, tree-structured hierarchical, symmetric, bi-orthogonal, and variable length LTs, are defined, and their properties and factorization schemes are

described. Generalized versions of the lapped orthogonal transform (LOT), called GenLOT, are developed in Sections 5.6.3–4 while cosine-modulated LTs, otherwise known as MLT or ELT, are discussed in Section 5.8. To demonstrate the promise and potential for LTs in image coding, well known image compression algorithms are applied to standard test images, with DCT or the wavelet transform replaced by LTs. Comparative analysis shows the elimination of ringing and blocking artifacts that are characteristic of the DCT based coders and also performance rivaling that of the wavelet transforms.

Chapter 6 Wavelet-Based Image Compression

This is another highly valuable chapter as it addresses wavelet-based image compression. Wavelet-based transforms give a time-frequency decomposition of the signal, which has multi-resolution characteristics. The transforms have superior energy compaction and compatibility with Human Visual System (HVS). They make possible the embedded bit-stream coding corresponding to various subbands (the basis for fast browsing of images or databases over the Internet). Discrete wavelet transforms (DWT) and its variants have been adopted both by the FBI in the use of fingerprint image compression and the international standards groups (JPEG-2000 and MPEG-4 still frame image coding). It is highly possible that wavelets may eventually replace DCT in all the coders. Walker and Nguyen provide a clear explanation of the multiresolution aspects of DWT and its implementation using a 2-channel filter bank. Some of the recent enhancements of the basic DWT, such as EZW, SPIHT, WDR, and ASWDR, are enumerated, followed by their implementation in image coding and subsequent evaluation. Various Web sites that provide software, literature, simulation results, and innumerable other details further strengthen the chapter's utility.

Chapter 7 Fractal-Based Image and Video Compression

The concepts and techniques of fractal-based image/video compression are introduced in this chapter by Lu. The seminal work by Mandelbrot forms the basis of many treatises of fractal applications, made popular by movie scenes generated graphically by the use of fractals. Fractal-based signal analysis is currently at the forefront of research. Although compression techniques based on affine transforms or iterated function systems (IFS) may not have caught the attention of every researcher, their attractive properties making possible high compression ratios and asymmetric coding certainly deserve further study. With the advent of super HDTV, wireless cellular multimedia phones, and interactive services on the Internet, fractal transform and its variants such as IFS, QPIFS, and PIFS will find their rightful place in the compression arena. Starting with the basic properties of fractals, Lu demonstrates the compression property of fractals using the encoding/decoding procedures. The capabilities of fractals are illustrated using images and video. As with the other chapters, Web and ftp sites, mostly maintained by universities, provide access to software, literature, products, R&D, and applications to the interested readers.

Chapter 8 Compression of Wavelet Transform Coefficients

The concluding chapter presents a philosophical and thoughtful argument for the effectiveness of transforms in general and wavelets in particular for bandwidth reduction. The superiority of wavelet transform over others, including the widely used DCT, is clearly demonstrated by the characteristics of the DWT. From the chapter's title, the reader may get a wrong impression of duplication with Chapter 6. On the contrary, this chapter complements the topics in Chapter 6 by a clear exposition of the superior performance of the DWT over other transforms. The subband decomposition inherent in dyadic wavelet transform, preservation of spatial signal features in subbands of different scales, and self similarities among subbands of the spatial orientation are some of the reasons for this superiority. These self-similarities are conducive to statistical context modeling and adaptive entropy coding of wavelet coefficients. By a lucid presentation of these concepts aided by implementation on test images, Wu convincingly demonstrates the validity of the DWT adopted in JPEG-2000 and MPEG-4 and the bright future it has in other applications.

Acknowledgements

The editors have been entrusted with the organizational and administrative process in compiling this handbook. Needless to say, without the expertise and efforts of the individual chapter authors, this handbook would never have seen the light of day. The editors sincerely acknowledge the energetic contributions from the chapter authors, whose uniform excellence has made this an outstanding volume. The editors thank the authors for their prompt and timely responses in spite of their heavy commitments in their daily academic or professional lives. It is hoped that the completion of this handbook will elicit a sense of pride and accomplishment, a well-earned and well-deserved reward for their efforts. The editors would also like to thank their families for the patience and perseverance they showed during the months of preparation of this handbook.

List of Acronyms

AFB	Analysis filter bank
ASPEC	Audio spectral perceptual entropy coding
ASWDR	Adaptively scanned wavelet difference reduction
bpp	Bits per pixel
CREW	Compression by reversible embedded wavelets
DCT	Discrete cosine transform
DFT	Discrete Fourier transform
DPCM	Differential pulse code modulation
DSP	Digital signal processing
DST	Discrete sine transform
DTFT	Discrete time Fourier transform
DWP	Discrete wavelet packet
DWT	Discrete wavelet transform
ECECOW	Embedded conditional entropy coding of wavelet
ECG	Electrocardiogram
ELT	Extended lapped transform
EZC	Embedded zerotree coding
EZW	Embedded zerotree wavelet
FAQ	Frequently asked questions
FFT	Fast Fourier transform
FIR	Finite impulse response
FLT	Fast lapped transform
FoF	Fear of functionality
FPGA	Field programmable gate array
GenLOT	Generalized LOT
GNU	GNU's Not Unix
GNUX	GNU-Linux
H.261	Standard for compression of videotelephony and teleconferencing
H.263	Standard for visual communication via telephone lines
HDTV	High definition TV
HLT	Hierarchical lapped transform
HSI	Hue, saturation, intensity
HV	Horizontal vertical
HVS	Human visual system
IDFT	Inverse discrete Fourier transform
IFS	Iterated function systems

ISO	International Standards Organization
ITU	International Telecommunication Union
JBIG	Joint Binary Image Group
JPEG	Joint Photographic Experts Group
JPEG-LS	JPEG-Lossless
KLT	Karhunen-Loève transform
LBT	Lapped bi-orthogonal transform
LOT	Lapped orthogonal transform
LT	Lapped transform
LZC	Layered zero coding
MC	Motion compensated
MDCT	Modified discrete cosine transform
MDST	Modified discrete sine transform
MIMO	Multi-input multi-output
MLT	Modulated lapped transform
MOS	Mean opinion score
MP3	MPEG-Layer 3
MPEG	Moving Pictures Expert Group
MPEG-AAC	MPEG advanced audio coder
MSE	Mean squares error
PAC	Perceptual audio coder
PCA	Principal component analysis
PIFS	Partitioned iterated function systems
PR	Perfect reconstruction
PSD	Personal safety device
PSNR	Peak signal to noise ratio
PTM	Polyphase transfer matrix
PTP	Picture transfer protocol
QCLS	Quadratic-constrained least squares
QM	Cute sound
QPIFS	Quadtree partitioned iterated function systems
RGB	Red, green, and blue
RLC	Run-length coding
RLD	Run-length decoder
ROI	Region of interest
RTT	Round trip time
SDF	Symmetric delay factorization
SFB	Synthesis filter bank
SPIHT	Set partitioning of hierarchical tree
STW	Spatial orientation tree wavelet
SVD	Singular value decomposition
TDAC	Time domain aliasing cancellation
TF	Time-frequency
VLC	Variable-length coding
VLD	Variable-length decoder
VQ	Vector quantization
WDR	Wavelet difference reduction
YIQ	Luminance, in-phase, and quadrature-phase chrominance

Contributors

Vladimir Britanak Institute of Control Theory and Robotics, Slovak Academy of Sciences, Bratislava, Slovak Republic

Ricardo L. de Queiroz Digital Imaging Technology Center, Xerox Corporation, Webster, New York

R.D. Dony School of Engineering, University of Guelph, Guelph, Ontario, Canada

Guojun Lu Gippsland School of Computing and Information Technology, Monash University, Churchill, Victoria, Australia

Steve Mann Department of Electrical and Computer Engineering, University of Toronto, Toronto, Ontario, Canada

Truong Q. Nguyen Department of Electrical and Computer Engineering, Boston University, Boston, Massachusetts

Gerald Schuller Bell Labs, Lucent Technologies, Murray Hill, New Jersey

Ivan W. Selesnick Department of Electrical Engineering, Polytechnic University, Brooklyn, New York

Trac D. Tran Department of Electrical and Computer Engineering, The Johns Hopkins University, Baltimore, Maryland

James S. Walker Department of Mathematics, University of Wisconsin-Eau Claire, Eau Claire, Wisconsin

Xiaolin Wu Department of Computer Science, University of Western Ontario, London, Ontario, Canada

Contents

1 Karhunen-Loève Transform

- 1.1 Introduction
- 1.2 Data Decorrelation
 - 1.2.1 Calculation of the KLT
- 1.3 Performance of Transforms
 - 1.3.1 Information Theory
 - 1.3.2 Quantization
 - 1.3.3 Truncation Error
 - 1.3.4 Block Size
- 1.4 Examples
 - 1.4.1 Calculation of KLT
 - 1.4.2 Quantization and Encoding
 - 1.4.3 Generalization
 - 1.4.4 Markov-1 Solution
 - 1.4.5 Medical Imaging
 - 1.4.6 Color Images
- 1.5 Summary
- References

2 The Discrete Fourier Transform

- 2.1 Introduction
- 2.2 The DFT Matrix
- 2.3 An Example
- 2.4 DFT Frequency Analysis
- 2.5 Selected Properties of the DFT
 - 2.5.1 Symmetry Properties
- 2.6 Real-Valued DFT-Based Transforms
- 2.7 The Fast Fourier Transform
- 2.8 The DFT in Coding Applications
- 2.9 The DFT and Filter Banks
 - 2.9.1 Cosine-Modulated Filter Banks
 - 2.9.2 Complex DFT-Based Filter Banks

- 2.10 Conclusion
- 2.11 FFT Web sites
- References

3 Comparametric Transforms for Transmitting Eye Tap Video with Picture Transfer Protocol (PTP)

- 3.1 Introduction: Wearable Cybernetics
 - 3.1.1 Historical Overview of WearComp
 - 3.1.2 Eye Tap Video
- 3.2 The Edgertonian Image Sequence
 - 3.2.1 Edgertonian versus Nyquist Thinking
 - 3.2.2 Frames versus Rows, Columns, and Pixels
- 3.3 Picture Transfer Protocol (PTP)
- 3.4 Best Case Imaging and Fear of Functionality
- 3.5 Comparametric Image Sequence Analysis
 - 3.5.1 Camera, Eye, or Head Motion: Common Assumptions and Terminology
 - 3.5.2 VideoOrbits
- 3.6 Framework: Comparameter Estimation and Optical Flow
 - 3.6.1 Feature-Based Methods
 - 3.6.2 Featureless Methods Based on Generalized Cross-Correlation
 - 3.6.3 Featureless Methods Based on Spatio-Temporal Derivatives
- 3.7 Multiscale Projective Flow Comparameter Estimation
 - 3.7.1 Four Point Method for Relating Approximate Model to Exact Model
 - 3.7.2 Overview of the New Projective Flow Algorithm
 - 3.7.3 Multiscale Repetitive Implementation
 - 3.7.4 Exploiting Commutativity for Parameter Estimation
- 3.8 Performance/Applications
 - 3.8.1 A Paradigm Reversal in Resolution Enhancement
 - 3.8.2 Increasing Resolution in the “Pixel Sense”
- 3.9 Summary
- 3.10 Acknowledgements
- References

4 Discrete Cosine and Sine Transforms

- 4.1 Introduction
- 4.2 The Family of DCTs and DSTs
 - 4.2.1 Definitions of DCTs and DSTs
 - 4.2.2 Mathematical Properties
 - 4.2.3 Relations to the KLT
- 4.3 A Unified Fast Computation of DCTs and DSTs
 - 4.3.1 Definitions of Even-Odd Matrices
 - 4.3.2 DCT-II/DST-II and DCT-III/DST-III Computation
 - 4.3.3 DCT-I and DST-I Computation

- 4.3.4 DCT-IV/DST-IV Computation
- 4.3.5 Implementation of the Unified Fast Computation of DCTs and DSTs
- 4.4 The 2-D DCT/DST Universal Computational Structure
 - 4.4.1 The Fast Direct 2-D DCT/DST Computation
 - 4.4.2 Implementation of the Direct 2-D DCT/DST Computation
- 4.5 DCT and Data Compression
 - 4.5.1 DCT-Based Image Compression/Decompression
 - 4.5.2 Data Structures for Compression/Decompression
 - 4.5.3 Setting the Quantization Table
 - 4.5.4 Standard Huffman Coding/Decoding Tables
 - 4.5.5 Compression of One Sub-Image Block
 - 4.5.6 Decompression of One Sub-Image Block
 - 4.5.7 Image Compression/Decompression
 - 4.5.8 Compression of Color Images
 - 4.5.9 Results of Image Compression
- 4.6 Summary
- References

5 Lapped Transforms for Image Compression

- 5.1 Introduction
 - 5.1.1 Notation
 - 5.1.2 Brief History
 - 5.1.3 Block Transforms
 - 5.1.4 Factorization of Discrete Transforms
 - 5.1.5 Discrete MIMO Linear Systems
 - 5.1.6 Block Transform as a MIMO System
- 5.2 Lapped Transforms
 - 5.2.1 Orthogonal Lapped Transforms
 - 5.2.2 Nonorthogonal Lapped Transforms
- 5.3 LTs as MIMO Systems
- 5.4 Factorization of Lapped Transforms
- 5.5 Hierarchical Connection of LTs: An Introduction
 - 5.5.1 Time-Frequency Diagram
 - 5.5.2 Tree-Structured Hierarchical Lapped Transforms
 - 5.5.3 Variable-Length LTs
- 5.6 Practical Symmetric LTs
 - 5.6.1 The Lapped Orthogonal Transform: LOT
 - 5.6.2 The Lapped Bi-Orthogonal Transform: LBT
 - 5.6.3 The Generalized LOT: GenLOT
 - 5.6.4 The General Factorization: GLBT
- 5.7 The Fast Lapped Transform: FLT
- 5.8 Modulated LTs
- 5.9 Finite-Length Signals
 - 5.9.1 Overall Transform

- 5.9.2 Recovering Distorted Samples
- 5.9.3 Symmetric Extensions
- 5.10 Design Issues for Compression
- 5.11 Transform-Based Image Compression Systems
 - 5.11.1 JPEG
 - 5.11.2 Embedded Zerotree Coding
 - 5.11.3 Other Coders
- 5.12 Performance Analysis
 - 5.12.1 JPEG
 - 5.12.2 Embedded Zerotree Coding
- 5.13 Conclusions
- References

6 Wavelet-Based Image Compression

- 6.1 Introduction
- 6.2 Dyadic Wavelet Transform
 - 6.2.1 Two-Channel Perfect-Reconstruction Filter Bank
 - 6.2.2 Dyadic Wavelet Transform, Multiresolution Representation
 - 6.2.3 Wavelet Smoothness
- 6.3 Wavelet-Based Image Compression
 - 6.3.1 Lossy Compression
 - 6.3.2 EZW Algorithm
 - 6.3.3 SPIHT Algorithm
 - 6.3.4 WDR Algorithm
 - 6.3.5 ASWDR Algorithm
 - 6.3.6 Lossless Compression
 - 6.3.7 Color Images
 - 6.3.8 Other Compression Algorithms
 - 6.3.9 Ringing Artifacts and Postprocessing Algorithms
- References

7 Fractal-Based Image and Video Compression

- 7.1 Introduction
- 7.2 Basic Properties of Fractals and Image Compression
- 7.3 Contractive Affine Transforms, Iterated Function Systems, and Image Generation
- 7.4 Image Compression Directly Based on the IFS Theory
- 7.5 Image Compression Based on IFS Library
- 7.6 Image Compression Based on Partitioned IFS
 - 7.6.1 Image Partitions
 - 7.6.2 Distortion Measure
 - 7.6.3 A Class of Discrete Image Transformation
 - 7.6.4 Encoding and Decoding Procedures
 - 7.6.5 Experimental Results
- 7.7 Image Coding Using Quadtree Partitioned IFS (QPIFS)

- 7.7.1 RMS Tolerance Selection
- 7.7.2 A Compact Storage Scheme
- 7.7.3 Experimental Results
- 7.8 Image Coding by Exploiting Scalability of Fractals
 - 7.8.1 Image Spatial Sub-Sampling
 - 7.8.2 Decoding to a Larger Image
 - 7.8.3 Experimental Results
- 7.9 Video Sequence Compression using Quadtree PIFS
 - 7.9.1 Definitions of Types of Range Blocks
 - 7.9.2 Encoding and Decoding Processes
 - 7.9.3 Storage Requirements
 - 7.9.4 Experimental Results
 - 7.9.5 Discussion
- 7.10 Other Fractal-Based Image Compression Techniques
 - 7.10.1 Segmentation-Based Coding Using Fractal Dimension
 - 7.10.2 Yardstick Coding
- 7.11 Conclusions
- References

8 Compression of Wavelet Transform Coefficients

- 8.1 Introduction
- 8.2 Embedded Coefficient Coding
- 8.3 Statistical Context Modeling of Embedded Bit Stream
- 8.4 Context Dilution Problem
- 8.5 Context Formation
- 8.6 Context Quantization
- 8.7 Optimization of Context Quantization
- 8.8 Dynamic Programming for Minimum Conditional Entropy
- 8.9 Fast Algorithms for High-Order Context Modeling
 - 8.9.1 Context Formation via Convolution
 - 8.9.2 Shared Modeling Context for Signs and Textures
- 8.10 Experimental Results
 - 8.10.1 Lossy Case
 - 8.10.2 Lossless Case
- 8.11 Summary
- References